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M.Sc. (First Semester) Examination, 2025

PHYSICS

Paper : Second

(Classical Mechanics)

Time : Two Hours ] [ Maximum Marks : 75

Note : Attempt all sections as per instructions.

Section-A

(Very Short Answer Type Questions)

Note : Attempt all the (05) five questions.

Each question carries 02 (two) marks and answer of each question should not exceed 50 words.  $5 \times 2 = 10$

1. (a) Define generalised coordinate.

(b) What is Hamilton's principle?

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(c) What are advantages of canonical transformation?

(d) Explain Poisson bracket.

(e) Define action angle variable.

Section-B

(Short Answer Type Questions)

Note : Attempt any 05 (Five) questions out of Total 08 (Eight) questions. Each question carries 05 (five) marks and answer of each question should not exceed 100 words.  $5 \times 5 = 25$

2. (a) Write the Lagrange's equation of motion for a particle of mass  $m$  falling under gravity.

(b) Obtain Hamiltonian of a charged particle in an electromagnetic field.

(c) Show that the transformation :

$$P = \frac{1}{2}(p^2 + q^2)$$

$$Q = \tan^{-1}\left(\frac{q}{p}\right) \text{ is canonical.}$$

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- (d) What is principle of least action?  
(e) Deduce Hamilton-Jacobi Equation.  
(f) Discuss the theory of spinning symmetrical top under gravity.  
(g) Explain theory of small oscillation.  
(h) Derive equation of motion in terms of Poisson's Bracket.

**Section-C**

**(Long Answer Type Questions)**

**Note :** Attempt any **02 (Two)** questions out of total **04 (four)** questions. Each question carries **20 (twenty)** marks and answer of each question should not exceed **400** words.  $2 \times 20 = 40$

3. (a) Find the Lagrange's equation of motion using D' Alembert's principle for holonomic system. Show that if the Lagrangian does not depend explicitly on time, then the energy is conserved.

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- (b) Deduce the principle of least actions in the following form :

$$\delta \int_{t_1}^{t_2} T dt = 0$$

- Where T is the kinetic energy.

- (c) State and prove Liouville's theorem. Give the physical significance of this theorem.

- (d) Discuss the vibrations of a linear symmetric triatomic molecule and calculate the eigen vectors for the three modes of vibrations for  $\omega_1 = 0$ ,  $\omega_2 = \sqrt{\frac{k}{m}}$ , and  $\omega_3 = \sqrt{\frac{k}{m} \left(1 + \frac{2m}{M}\right)}$  where middle atom mass is M and atoms at end have mass m and k is the spring force constant.

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